Abstract

The paper goes back to the original insight by Phillips and investigates the negative relationship between money wage inflation and the unemployment rate occurring at frequency bands that stretch beyond those of the business cycle. We use UK annual data for the period 1861-2015, and post-WWII quarterly data from 1960 to 2016. The two critical findings are that the wage Phillips Curve is predominantly a medium-run phenomenon, comprised in the 8-to16-year frequency band, and that the curve disappears beyond this range. Similar conclusions are reached using the post-WWII quarterly sample: at the aggregate level and at high frequencies the PC relationship is unstable over time, whereas in the frequency range between 32 to 64 quarters (our medium run timescale), this time dependency disappears.

Keywords: Phillips Curve, frequency bands, wavelet, medium run

JEL classification codes: E00, E30, E31, E32.
1 Introduction

Sixty-one years after A.W. Phillips 1958 published the “The relation between unemployment and the rate of change money wage rates in the United Kingdom, 1861-1957”, the empirical validity of its Curve (PC for short) remains a hotly debated issue both in the world of academic research and policy applications. The vastness of the contributions defies any attempt to provide a comprehensive review of the literature; a short list of the highlights of this research includes Samuelson and Solow (1960), Phelps (1967), Friedman (1968), Lucas (1972, 1973), Sargent and Wallace (1975), Gordon (1982, 2011), King and Watson (1994), Galí and Gertler (1999), Staiger et al. (1997a,b), Haldane and Quah (1999), Mankiw (2001), Mavroeidis et al. (2014), Galí (2011) and Hall and Sargent (2018).

Much of this research, possibly reflecting the influence of Samuelson and Solow (1960) on the economics profession, was done focusing on price inflation rather than wage inflation. That held true also in the policy world. A very early policy application of the PC was the Kennedy-Johnson tax cuts of 1964 and 1965 in the US, the objective being to reduce the unemployment rate to 4 per cent (Economic Report of the President (1962, p.46). Accordin to Walter Heller 1964, p.237, the then chairman of the President’s Council of Economic Advisers, “… we cannot say we have a conclusive test of our 4 per cent full-employment bench mark and its attendant Phillips curve assumptions. What we can say is: so far, so good, adding that the 5-percenteres have already been proved wrong, while we (interim) 4-per- centers have not. And the progressive stepup in manpower programs…may well be reducing the critical unemployment level at which we have to choose between further shrinkage of unemployment and accelerating increases in the price level.”

Also central banks did accept the relevance of the relationship between rates of inflation and level of real economic activity (Mavroeidis et al., 2014, p.124), despite evidence that the relationship had shifted and become less reliable over time (Blanchard et al., 2015; BIS (2017, p. 63-67); Carney, 2017; Cunliffe, 2017; FOMC, 2018).3

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1It includes also the report written by the President’s Council of Economic Advisers which included high-caliber Keynesian economists James Tobin, Arthur Okun and Otto Eckstein
2But, as (Gordon, 2011, p.14-15) notes, “the zero-inflation unemployment rate was higher than 4 percent and the tax cuts would have implied an acceleration of inflation even without the further loosening of the fiscal floodgates due to the Vietnam War.”
3The durability of the PC in the literature can be assessed with the use of scholarly search engines. According to EconLit, 674 scholarly journal articles have PC in the document title (search date: March 4, 2018). The data bank of RePEc (Research Papers in Economics) listed, on the same date, 1,019 articles and 1,669 working papers mentioning “Phillips Curve” in their abstract. In a Google Scholar search, done again on the same date, the response to the query “Phillips Curve is vertical” was 431,000 documents. “Phillips Curve is dead” 94,000, “Phillips Curve and central banking” 55,500, “Phillips Curve is steeper” 55,100, “Phillips Curve is alive” 32,700, “Phillips Curve is flatter” 22,100.
This paper goes back to the origin and focuses on the negative relationship between money wage inflation and the unemployment rate occurring at frequency bands stretching beyond the business cycle. Our point of departure is Phillips’ unorthodox data transformation, consisting in reducing the 53 observations from 1861 to 1913—rearranged in ascending order in terms of the unemployment rate—in six average values of arbitrarily selected intervals, which were used to estimate the hyperbola, \[ \Delta w = -0.90 + 9.64 \cdot U^{-1.39}, \] where \( \Delta w \) denotes the rate of change of money wages and \( U \) = the rate of unemployment.\(^{4}\) Phillips dismissed price inflation as a contributing factor for his empirical model arguing that an excess demand for labor would have induced firms to bid up money wages independently of inflation. This assumption and the restriction that changes in unemployment were essentially set to zero by averaging observations over the selected time intervals suggests that Phillips was interested in a long-run relationship (Desai, 1975).\(^{5}\) Phillips’ procedure was unfamiliar to economists of the time, but today can be interpreted as a simple moving average with non-overlapping variable-width windows. Since a moving average removes high-frequency fluctuations of the time series, Phillips’ averaging procedure is somewhat equivalent to applying a low-pass filter to the data. In brief, Phillips performed a crude form of wavelet analysis (Gallegati et al., 2011, footnote 2; Gallegati and Ramsey, unpublished). The more popular replication of the PC by Lipsey (1960) relied, instead, on familiar aggregated time-scale estimation techniques. It “became the standard method of analysis in economics by 1960...[and] inspired a booming industry in Phillips curve estimation” (Wulwick, 1996, p.410).

Wavelet methodology was applied by Gallegati et al. (2011) to estimate the wage PC for the US along time and frequency domain. Under this methodology, one first decomposes the variables of interest into their time-scale components and then estimates the PC on a scale-to-scale level (disaggregation by frequency bands) so as to study simultaneously statistical properties in both time and frequency domain. Using the same methodology, we will revisit Phillips’ original PC in the UK. The data will be Phillips’ own and an expansive annual and quarterly samples.

\(^{4}\) For subsequent periods, the intercepts of the curves were adjusted by hand using the estimate of the 1861-1913 years.

\(^{5}\) Phillips’ argument goes as follows: “For suppose that productivity is increasing steadily at a rate of, say, 2 per cent per annum and that aggregate demand is increasing similarly so that unemployment is remaining constant at say, 2 per cent. Assume that with this level of unemployment and without any cost of living adjustment wage rates rise by, say, 3 per cent per annum as a result of employers’ competitive for labour and that import prices and the prices of other factor services are also rising by 3 per cent per annum. Then retail prices will be rising on average at the rate of 1 per cent per annum...Under these conditions the introduction of cost of living adjustments in wage rates will have no effect, for employers will merely be giving under the name of cost of living adjustment part of the wage increases which they would in any case have given as a result of their competitive bidding for labour.” (p.284).
The main motivation of the paper is not to assess the time dependency (or temporal instability) of the PC, which is a dominant aspect in literature, but its frequency dependency (or frequency instability). To this end we perform two exercises. The first is to replicate the original work by Phillips using the modern wavelet technology with the intent to corroborate that the PC is a medium-run relationship between money wage inflation and the rate of unemployment instead of a short-run tradeoff, as postulated by Samuelson and Solow (1960). A medium-run PC relationship would refute the notion of an exploitable short-run tradeoff between inflation and unemployment. The second is to extend the analysis beyond the original sample to check whether the medium-run PC survives till present days. Our expanded data set goes from 1861 to 2015 for yearly observations and from 1960:Q1 to 2016:Q4 for quarterly observations.

Our main findings are that, for the period 1861-1913, Phillips detected a negative relationship between wage inflation and unemployment that is mainly present beyond a business-cycle frequency band. This medium-run relationship, not only emerges from the original Phillips dataset, but survives until present days using a long stretch of historical annual data. The other significant finding is that the curve disappears in the long run. Similar conclusions are reached for the post-WWII quarterly data: at the aggregate level and at high frequencies the PC relationship is unstable over time. But, in the frequency range between 32 to 64 quarters (our medium run timescale), this dependency disappears.

The structure of the paper is as follows. We start in Section 2 by estimating a canonical PC relationship at the aggregate level, that is with crude data and ignoring a decomposition in frequency bands. In Section 3 we analyze the PC in time-frequency domain over the long stretch of annual data, and estimate wage PCs at different time-scales and over different time intervals. We repeat the exercise for post-WWII quarterly data in Section 4. Section 5 discusses the significance of our findings in relation to the literature. Conclusions are drawn in Section 6. An Appendix contains a description of the data, with accompanying graphs, and a concise summary of wavelet analysis.

2 The canonical PC

We start our empirical work estimating a canonical PC relationship at the aggregate level, that is with crude data and ignoring a decomposition in frequency bands. Our specification follows Staiger et al. (1997a,b):

\[ \Delta w_t = \alpha_0 + \alpha_1 U_t + \alpha_2 \Delta LP_t + \alpha_3 \pi_t + \alpha_4 CTR_t + \epsilon_t \]  

(1)
where $\Delta w_t =$ first difference of the delta log of the money wage rate, $U_t =$ the rate of unemployment, $\Delta LP_t =$ delta log of labor productivity, $\pi_t =$ price inflation, $CTR_t =$ control variables, and $\epsilon_t =$ error term.

The nominal wage rate is measured as the composite average of weekly earnings; labor productivity is measured as output per hour worked, and price inflation is measured in terms of the GDP deflator at market prices. All data come from The Bank of England’s collection of historical macroeconomic and financial statistics; see Ryland et al. (2010) and the Appendix for details. Controls are defined as dummy variables: WWI stands for the first world war years (1914-1918), GD for the Great Depression years (1929-1933), WWII for the second world war years (1939-1945), Oil for the two oil shocks of the Seventies (1973-1980) and GFC for the Great Financial Crisis years (2007-2010).

Table 1 displays estimates of the $\alpha$ coefficients in Equation 1, except for the intercept, with their associated standard errors adjusted for possible serial correlation and heteroskedacity in the error term. Four samples are considered: the longest sample, 1861-2015, the Phillips’ sample, 1861-1913, the interwar period, 1923-1948, and the post-WWII era (1960-2015). The salient findings are that the PC effect, the impact of the rate of unemployment on wage inflation is statistically significant (at least at the 5 percent confidence level) only in the pre-WWI period: Phillips was judicious, or lucky, in selecting the sample. For the rest, the PC, with aggregate data, is time dependent. That is, PC, with aggregate data, is time dependent. The rate of price inflation is statistically significant in all periods, except in the Phillips’ period, thus confirming the original outcome that prices were not relevant in the PC. The coefficient of $\pi_t$ is statistically not different from unity in the post-WWII period and very close to unity in the expansive sample, a result that is consistent with a vertical PC (Benati, 2015). There is some evidence that the war years raised wage inflation, while the Great Financial Crisis lowered them.

Table 2 presents the quarterly estimates of Equation 1 for the post-WWII period. Four time windows of expanding size are considered: 1990-2016, 1980-2016, 1970-2016, and 1960-2016. In all four cases, the quarterly estimates are in line with the post-WWII annual estimates of Table 1: no variable is statistically significant, again at the 5 percent confidence level, with the exception of price inflation, a finding that is consistent with those reported by Gallegati et al. (2011) for the US.
### Table 1: Dependent Variable: $\Delta w_t$, Bank of England, annual data, 1861-2015

<table>
<thead>
<tr>
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<tbody>
<tr>
<td>$U_t$</td>
<td>-0.095</td>
<td>-0.622</td>
<td>-0.042</td>
<td>-0.089</td>
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<tr>
<td></td>
<td>(0.082)</td>
<td>(0.116)</td>
<td>(0.072)</td>
<td>(0.068)</td>
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<tr>
<td>$\Delta LP_t$</td>
<td>0.371</td>
<td>-0.091</td>
<td>0.523</td>
<td>0.226</td>
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<tr>
<td></td>
<td>(0.076)</td>
<td>(0.083)</td>
<td>(0.109)</td>
<td>(0.122)</td>
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<tr>
<td>$\pi_t$</td>
<td>0.834</td>
<td>0.225</td>
<td>0.735</td>
<td>0.923</td>
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<td>(0.082)</td>
<td>(0.116)</td>
<td>(0.088)</td>
<td>(0.101)</td>
</tr>
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<td>WWI</td>
<td>0.064</td>
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<tr>
<td></td>
<td>(0.010)</td>
<td></td>
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<tr>
<td>GD</td>
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<td></td>
<td>(0.007)</td>
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<tr>
<td>WWII</td>
<td>0.009</td>
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<tr>
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<td>(0.005)</td>
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<tr>
<td>OIL</td>
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<tr>
<td></td>
<td>(0.012)</td>
<td></td>
<td>(0.015)</td>
<td></td>
</tr>
<tr>
<td>GFC</td>
<td>-0.002</td>
<td></td>
<td>-0.013</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.004)</td>
<td></td>
<td>(0.005)</td>
<td></td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.863</td>
<td>0.553</td>
<td>0.907</td>
<td>0.882</td>
</tr>
<tr>
<td>$\mathcal{L}$</td>
<td>386.2</td>
<td>173.9</td>
<td>78.06</td>
<td>154.3</td>
</tr>
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</table>

Coefficients in bold are significant at a 5 % level. Standard errors are robust to autocorrelation and heteroskedasticity using an HAC estimator for the variance and covariance matrix.

### Table 2: Dependent Variable: $\Delta w_t$, Bank of England, quarterly data, 1960:1-2016:4

<table>
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<tr>
<th></th>
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</thead>
<tbody>
<tr>
<td>$U_t$</td>
<td>-0.104</td>
<td>-0.103</td>
<td>-0.129</td>
<td>-0.104</td>
</tr>
<tr>
<td></td>
<td>(0.134)</td>
<td>(0.135)</td>
<td>(0.092)</td>
<td>(0.134)</td>
</tr>
<tr>
<td>$\Delta LP_t$</td>
<td>0.179</td>
<td>0.029</td>
<td>-0.015</td>
<td>0.046</td>
</tr>
<tr>
<td></td>
<td>(0.170)</td>
<td>(0.155)</td>
<td>(0.136)</td>
<td>(0.136)</td>
</tr>
<tr>
<td>$\pi_t$</td>
<td>0.268</td>
<td>0.622</td>
<td>0.681</td>
<td>0.717</td>
</tr>
<tr>
<td></td>
<td>(0.134)</td>
<td>(0.073)</td>
<td>(0.083)</td>
<td>(0.083)</td>
</tr>
<tr>
<td>OIL</td>
<td>2.168</td>
<td>2.927</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(1.371)</td>
<td>(1.420)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>GFC</td>
<td>-1.465</td>
<td>-2.216</td>
<td>-2.790</td>
<td>-2.831</td>
</tr>
<tr>
<td></td>
<td>(0.887)</td>
<td>(0.962)</td>
<td>(0.902)</td>
<td>(0.824)</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.061</td>
<td>0.381</td>
<td>0.570</td>
<td>0.521</td>
</tr>
<tr>
<td>$\mathcal{L}$</td>
<td>-278.6</td>
<td>-388.1</td>
<td>-528.6</td>
<td>-638.4</td>
</tr>
</tbody>
</table>

Coefficients in bold are significant at a 5 % level. Standard errors are robust to autocorrelation and heteroskedasticity using an HAC estimator for the variance and covariance matrix.
Figure 1: Wage inflation and unemployment, annual data, aggregate frequencies

Figure 2: Wage inflation and unemployment, quarterly data, aggregate frequencies
We use a rolling window using the % 25 of the observations. Standard errors are robust to autocorrelation and heteroskedasticity using an HAC estimator for the variance and covariance matrix.

Figures 1 and 9 provide an intuitive visual representation of regression results reported in Table 1 and 2. Using annual data and aggregate frequencies, the classical negative relationship between wage inflation and unemployment clearly emerges in the period 1861-1913 and during the interwar period (1923-1948). After WWII, such a relationship vanishes. Quarterly data strongly confirms this evidence in all the subsample taken into consideration (1960-1979, 1980-1999 and 2000-2016).

In order to check if our results depend by the particular sample used in the estimation, we run several rolling window regressions. Figures 3 and 4 display the series of variable coefficients against time for annual and quarterly data, respectively. These coefficients are the estimates of rolling regressions with a window consisting of 25 percent of the total annual data and 50 percent of the total quarterly data. The windows are moved forward by an observation so that we can plot a continuous line of estimated coefficients for
the unemployment rate, productivity growth and the rate of inflation. The coefficient lines are surrounded by a confidence band set at 1.96 times the standard error.

For annual data, the PC relationship holds in the pre-WWI period and then disappears; for quarterly data it holds in the 1960s and then disappears. These results confirm that the relationship between money wage inflation and the unemployment rate, with aggregate data, suffers from a high degree of time dependency. Time dependency holds also for the coefficient of labor productivity. The impact of price inflation on wage inflation, instead, is consistently positive and tends towards unity under annual data.

3 PC in time-frequency domain over the long stretch

After the pioneering contribution of Daubechies (1992), the wavelet methodology has gained currency in analyzing time series, both in time and frequency domains, as an alternative to the standard passband filters (Baxter and King, 1999; Christiano and Fitzgerald, 2003). The advantages of the Daubechies wavelet filter is in the handling of non-stationary macroeconomic variables. In particular, the maximal overlap discrete wavelet transform (MODWT) is a compromise between continuous and discrete wavelet transforms with a relative ease of implementation and computational costs (Aguiar-Conraria and Soares, 2014). A brief review of wavelet analysis is provided in the Appendix.

MODWT decomposes a time series into different frequency bands. Table 3 shows a five-level decomposition that will be employed in our analysis: D1, for example, includes a range of 2 to 4 years for annual data and 2 to 4 quarters for quarterly data; D5, on the other extreme, is not defined for annual data, whereas for quarterly data includes a range 32 to 64 quarters. The business-cycle frequency band is defined by the range 2 to 8 years $A_1 = D_1 + D_2$, the medium run by $A_2 = D_3$, the range of 8 through 16 years; and the long run by $A_3$, the range beyond 16 years.

With MODWT we compute the wavelet coherence, a measure of the correlation strength between two time series. The intensity of this correlation is shown graphically by colors, going from intense blue (cold or low coherence) to red (hot or high coherence) against time and frequency range. A black contour line, called the cone of influence, defines the wavelet power at the 5 percent confidence level against the null hypothesis of white noise. The direction of arrows provides evidence, not only of a positive or negative coherence between two time series, but also of a leading or lagging pattern in the frequency and time domain. The
Table 3: Frequency domain interpretation in years of detail and approximation levels for a 5-level decomposition

<table>
<thead>
<tr>
<th>Detail level Dj</th>
<th>Quarterly data</th>
<th>Annual data</th>
</tr>
</thead>
<tbody>
<tr>
<td>D1</td>
<td>2-4 Q</td>
<td>2-4 Y</td>
</tr>
<tr>
<td>D2</td>
<td>4-8 Q</td>
<td>4-8 Y</td>
</tr>
<tr>
<td>D3</td>
<td>8-16 Q</td>
<td>8-16 Y</td>
</tr>
<tr>
<td>D4</td>
<td>16-32 Q</td>
<td></td>
</tr>
<tr>
<td>D5</td>
<td>32-64 Q</td>
<td></td>
</tr>
<tr>
<td>Trend</td>
<td>&gt; 64 Q</td>
<td>&gt; 16 Y</td>
</tr>
</tbody>
</table>

plots of the wavelet squared coherence were obtained using the MatLab package developed by Grinsted et al. (2004). According to this program, given two time series (X,Y), an arrow pointing to the North East signifies that Y leads X in phase (positive coherence), whereas an arrow pointing to the South East means that X leads Y in phase. The opposite is true for arrows pointing to the North West and the South West (negative coherence). Arrows pointing straight to the East and to the West signify positive and negative coherence with X and Y moving concomitantly.

To replicate Phillips, we use his original dataset reproduced in Wulwick (1996) and transform the data applying the continuous wavelet transform over the period 1861-1947; see panel (a) of Figure 5. In Panel (b) wage inflation is measured as in Equation 1, that is as the first difference of the logs. Panel (c) covers the entire sample 1856-2015. Compare first panels (a) and (b) of the figure. In both there is significant negative correlation in the 4 to 16 year range, but in (a) another significant correlation emerges in the lower 16 to 32 year range. This is due to Phillips’ definition of wage inflation, \((W_{t+1}-W_{t-1})/2W_t\), a centered first difference that smooths the series further than a traditional first difference. The coherence of the longest sample period in panel (c) confirms that the medium-run results hold both before and after WWII, whereas the long-run relation does not survive the post-WWII era.

Next, we perform a sequence of least square regressions at different frequency bands:

\[
\Delta w_t^{A_j} = \beta_0 + \beta_1 U_t^{A_j} + \beta_2 \Delta LP_t^{A_j} + \beta_3 \pi_t^{A_j} + \beta_4 CTR_t^{A_j} + \tau_t
\]  

(2)

where variables have the same meaning as in in equation (1); \(D_j\) (j =1,2,3) define the three frequency ranges discussed above—the business cycle \(A1 =
Figure 5: Coherence, original Phillips data transformation, 1861-1947, (left panel), original Phillips data (log deviation), 1861-1947, (middle panel), Bank of England Data, 1856-2016, (right panel)

(a) coherence(Δwt, Ut)
(b) coherence(Δwt, Ut)
(c) coherence(Δwt, Ut)

Time is recorded on the horizontal axis and the scale of the wavelet transform is recorded on the vertical axis with frequency converted to time units (quarters) to ease interpretation. The color code for power ranges from blue (low coherence) to red (high coherence). A pointwise significance test is performed against an almost process independent background spectrum. 90% confidence intervals for the null hypothesis that coherency is zero are plotted as contours in black in the figure. The cone of influence, represented by a shaded area corresponding to the region affected by edge effects, is marked by black lines.

$D_1 + D_2$, the medium run ($A_3 = D_3$), and the long run ($S_3$); $3$s are coefficients; and $\tau_t$ is an error term. Table 4 reports the estimates of Equation (2) over the entire sample, the pre-war WWI era (1861-1913), the interwar years (1923-1948), and the post-WWII period (1960-2015). Two strong results emerge. The first is that the wage PC is predominantly a medium-run phenomenon. In fact, the unemployment coefficient is negative, statistically significant and stable in all four time periods: ranging from -0.707 in the post-WWII era to -0.883 in the pre-WWI period. In contrast, at the business-cycle frequency, the $U$ negative coefficient is significant in the sub-sample estimated by Phillips but not in the other two. Even after WWI, a period that includes the sharp deflationary policy of the Bank of England to restore sterling to pre-war parity gold convertibility (Moggridge, 1969), the PC effect emerges primarily at the medium-run frequency.

The second is that the wage PC is vertical in the long run, an outcome occurring in the longest available sample (1861-2015), when we would expect a real variable such as unemployment to be invariant to all the varieties of monetary policies that have been carried for more than 150 years (Lucas, 1973; Hall and Sargent, 2018, p.126). To corroborate this point, the point estimate of the price inflation coefficient is 1.002 with a standard error of 0.06; cf. third
panel of Table 4. The case of a vertical wage PC is clearest when the impact of price inflation on wage inflation is unity. For the three sub-samples in the long-run time scale, price inflation is positive and statistically significant, but its estimates are either much less accurate than the one indicated above or differ from unity, or a unit price inflation coefficient occurs concomitantly with a non-zero unemployment coefficient.
Table 4: Wage PC time-scale regressions, annual data, 1861-2015

<table>
<thead>
<tr>
<th></th>
<th>Business cycle frequencies (D1+D2)</th>
<th>Medium run frequencies (D3)</th>
<th>Long run frequencies (S3)</th>
</tr>
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<tr>
<td>$U_t$</td>
<td></td>
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<tr>
<td></td>
<td>-0.719</td>
<td>-0.555</td>
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<td></td>
<td>(0.205)</td>
<td>(0.204)</td>
<td>(0.358)</td>
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<td>$LP_t$</td>
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<td></td>
<td>0.237</td>
<td>-0.108</td>
<td>0.463</td>
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<td>(0.079)</td>
<td>(0.081)</td>
<td>(0.118)</td>
</tr>
<tr>
<td>$\pi^{emoji}_{13}$</td>
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<tr>
<td></td>
<td>0.664</td>
<td>0.219</td>
<td>0.704</td>
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<tr>
<td></td>
<td>(0.094)</td>
<td>(0.106)</td>
<td>(0.065)</td>
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<td>$WWI$</td>
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<td></td>
<td>(0.005)</td>
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<tr>
<td>$GD$</td>
<td>0.0014</td>
<td>-0.000</td>
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<tr>
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<td>(0.003)</td>
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<td>$WWII$</td>
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<td>0.002</td>
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<td>(0.004)</td>
<td>(0.005)</td>
<td>(0.005)</td>
</tr>
<tr>
<td>$GFC$</td>
<td>0.000</td>
<td>-0.001</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.002)</td>
<td>(0.005)</td>
<td>(0.005)</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.591</td>
<td>0.246</td>
<td>0.640</td>
</tr>
<tr>
<td>$L$</td>
<td>443.6</td>
<td>170.4</td>
<td>75.80</td>
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</tbody>
</table>

Coefficients in bold are significant at a 5% level. Standard errors are robust to autocorrelation and heteroskedasticity using an HAC estimator for the variance and covariance matrix.
Figure 6 depicts the relationship between wage inflation and unemployment decomposed at different frequencies, business cycle (left column), medium run (middle column) and long run (left column). The decomposition highlights a weak relationship at the BC frequency, on the contrary, it appears to be strong in the medium run suggesting that the presence of the PC in the aggregate data is mainly due to the medium run frequency. This empirical finding holds for all the subsample.

In Figure 7 on rolling-window coefficients, the estimates show that, at a frequency band beyond 16 years (i.e. our long run), the vertical wage PC matches well with the unit tendency of the price inflation coefficient. In the medium run, instead, for almost half of the period a rising U coefficient is associated with a price inflation coefficient trending from unity towards zero.

Labor productivity growth impacts wage inflation in an unstable fashion: two out four coefficients are positive in the business-cycle range, one is significant in the medium-run range, and three are significantly positive and one is significantly negative in the long-run range. Figure 7 highlights the wandering time profile of the $\Delta LP$ coefficient. Particularly puzzling are the contrasting time profiles of labor productivity coefficients in the medium run and the long run; see the last two rows of Figure 7. We attribute these odd outcomes in part to measurement errors due, not only to poor data coverage, but also to objective difficulties in measuring overall labor productivity as the economy shifts, over the long stretch of 154 years, massive resources and inputs from agriculture to industry, from industry to services and finally from services to the so-called fourth industrial revolution of cyber-physical system interacting with the Internet of things and systems.
Figure 6: Wage inflation and unemployment, annual data, frequency decomposition

- Business cycle frequencies (D1+D2), 1861-1913
- Medium run frequencies (D3), 1861-1913
- Long run frequencies (S5), 1861-1913

- Business cycle frequencies (D1+D2), 1923-1948
- Medium run frequencies (D3), 1923-1948
- Long run frequencies (S5), 1923-1948

- Business cycle frequencies (D1+D2), 1958-2015
- Medium run frequencies (D3), 1958-2015
- Long run frequencies (S5), 1958-2015
Figure 7: Rolling window coefficients, UK, Bank of England, annual data, frequency decomposition, 1856-2016

We use a rolling window using the % 25 of the observations. Standard errors are robust to autocorrelation and heteroskedasticity using an HAC estimator for the variance and covariance matrix.
Time is recorded on the horizontal axis and the scale of the wavelet transform is recorded on the vertical axis with frequency converted to time units (quarters) to ease interpretation. The color code for power ranges from blue (low coherence) to red (high coherence). A pointwise significance test is performed against an almost process independent background spectrum. 90% confidence intervals for the null hypothesis that coherency is zero are plotted as contours in black in the figure. The cone of influence, represented by a shaded area corresponding to the region affected by edge effects, is marked by black lines.

4 The Post WWII PC

In this section we analyze now the period after the second world war in more detail, employing quarterly data from 1960 to 2016. Figure 8 displays the output of the continuous wavelet transform over the entire post-war period. The negative coherence between money wage inflation and unemployment is concentrated at the medium-run frequency (32 through 64 quarters), with few scattered red areas in the business-cycle range –1965-1972, 1972-1980 and 1997-2009–; see panel (a). Wage inflation is highly correlated with price inflation at the business-cycle timescale up to the mid-1990s and longer at the medium-run timescale. The growth of labor productivity appears to be less important for money inflation than either unemployment than price inflation.

Next, we repeat the same exercise we did for annual data:

\[
\Delta w_t^{D_j} = \delta_0 + \delta_1 U_t^{D_j} + \delta_2 \Delta LP_t^{D_j} + \delta_3 \pi_t^{D_j} + \delta_4 CTR_t^{D_j} + \kappa_t
\]  

where variables have the same meaning as in in Equation (2); \( D_j (j = 2, ..., 5) \) refer to the timescale details defined in Table 3; \( \delta s \) are coefficients; and \( \kappa_t \) is an error term. Table 5 reports the estimates of equation (3) over the entire sample 1960Q1-2016QIV and of three subsamples, each ten years shorter than the previous one. Separate regressions are performed for each timescale \( D_j (j = \ldots) \).
In addition, we report the estimates for the long-run timescale $S_5$ that goes beyond 64 quarters. The key findings are similar to those we found in the previous section. A negative and stable relationship between $\Delta w_t$ and $U_t$ occurs in the medium-run frequency $D_5$ (32 to 64 quarters). While the PC effect is also present in the business-cycle frequency $D_4$ (16 to 32 quarters), the pattern is time dependent. In fact, the rolling-window coefficients of Figure 10 show that the estimates of $\delta_{1-5}$ are on the whole negative, whereas the majority of the $\delta_{1-4}$ estimates is not statistically different from zero. The other important point is that the Phillips Curve is vertical in the long run. It is clearly the case with the estimates over the 1970Q1-2016Q4 and 1980Q1-2016Q4 periods (last row of Table 5).

Figure 9 shows the quarterly relationship between wage inflation and unemployment in the post WWII sample. At the business cycle frequencies, there is no clear evidence of the existence of the PC in all three subsamples (1960-1979, 1980-1999, 2000-2016). On the contrary, with the exception of the subsample 1960-1979, the PC strongly emerges at the medium run frequency.

---

$^6$PC effects at details $D_2$ and $D_3$ are even more erratic, swinging from positive to negative areas.
<table>
<thead>
<tr>
<th></th>
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</tr>
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<tbody>
<tr>
<td>$U^D_1$</td>
<td>0.460</td>
<td>-0.408</td>
<td>-0.825</td>
<td>-2.183</td>
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<tr>
<td>$\Delta L P^D_1$</td>
<td>0.058</td>
<td>0.149</td>
<td><strong>0.433</strong></td>
<td><strong>0.380</strong></td>
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<tr>
<td>$\pi^D_1$</td>
<td>-0.135</td>
<td>-0.145</td>
<td>-0.140</td>
<td>-0.142</td>
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<tr>
<td></td>
<td>(1.752)</td>
<td>(1.837)</td>
<td>(1.903)</td>
<td>(1.950)</td>
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<tr>
<td></td>
<td>(0.162)</td>
<td>(0.125)</td>
<td>(0.166)</td>
<td>(0.148)</td>
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<td></td>
<td>(0.115)</td>
<td>(0.098)</td>
<td>(0.119)</td>
<td>(0.103)</td>
</tr>
<tr>
<td>$U^D_2$</td>
<td>-0.539</td>
<td>-<strong>1.212</strong></td>
<td>0.160</td>
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<td>$\Delta L P^D_2$</td>
<td>0.275</td>
<td><strong>0.206</strong></td>
<td><strong>0.238</strong></td>
<td><strong>0.361</strong></td>
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<tr>
<td>$\pi^D_2$</td>
<td>-0.309</td>
<td>0.256</td>
<td><strong>0.823</strong></td>
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<tr>
<td></td>
<td>(0.369)</td>
<td>(0.483)</td>
<td>(0.609)</td>
<td>(0.580)</td>
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<tr>
<td></td>
<td>(0.113)</td>
<td>(0.074)</td>
<td>(0.074)</td>
<td>(0.068)</td>
</tr>
<tr>
<td></td>
<td>(0.066)</td>
<td>(0.135)</td>
<td>(0.189)</td>
<td>(0.176)</td>
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<tr>
<td>$U^D_3$</td>
<td>-<strong>1.171</strong></td>
<td>-0.150</td>
<td><strong>0.714</strong></td>
<td><strong>0.702</strong></td>
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<tr>
<td>$\Delta L P^D_3$</td>
<td>0.775</td>
<td><strong>0.569</strong></td>
<td><strong>0.631</strong></td>
<td><strong>0.671</strong></td>
</tr>
<tr>
<td>$\pi^D_3$</td>
<td>0.490</td>
<td>1.203</td>
<td><strong>1.257</strong></td>
<td><strong>1.264</strong></td>
</tr>
<tr>
<td></td>
<td>(0.162)</td>
<td>(0.191)</td>
<td>(0.312)</td>
<td>(0.277)</td>
</tr>
<tr>
<td></td>
<td>(0.058)</td>
<td>(0.082)</td>
<td>(0.109)</td>
<td>(0.071)</td>
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<tr>
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<td>(0.060)</td>
<td>(0.107)</td>
<td>(0.070)</td>
<td>(0.058)</td>
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<td>$U^D_4$</td>
<td>-<strong>0.644</strong></td>
<td>-0.679</td>
<td><strong>0.588</strong></td>
<td><strong>0.415</strong></td>
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<tr>
<td>$\Delta L P^D_4$</td>
<td>-0.422</td>
<td>-<strong>0.418</strong></td>
<td>-0.341</td>
<td>0.018</td>
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<tr>
<td>$\pi^D_4$</td>
<td>0.395</td>
<td><strong>0.283</strong></td>
<td><strong>0.266</strong></td>
<td><strong>0.531</strong></td>
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<tr>
<td></td>
<td>(0.068)</td>
<td>(0.070)</td>
<td>(0.109)</td>
<td>(0.133)</td>
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<tr>
<td></td>
<td>(0.112)</td>
<td>(0.105)</td>
<td>(0.177)</td>
<td>(0.234)</td>
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<td></td>
<td>(0.089)</td>
<td>(0.068)</td>
<td>(0.115)</td>
<td>(0.157)</td>
</tr>
<tr>
<td>$U^D_5$</td>
<td>-0.295</td>
<td>-0.046</td>
<td>-0.026</td>
<td><strong>0.028</strong></td>
</tr>
<tr>
<td>$\Delta L P^D_5$</td>
<td>1.071</td>
<td><strong>1.164</strong></td>
<td><strong>1.110</strong></td>
<td><strong>0.925</strong></td>
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<tr>
<td>$\pi^D_5$</td>
<td>1.347</td>
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<td><strong>0.947</strong></td>
<td><strong>0.971</strong></td>
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<td></td>
<td>(0.009)</td>
<td>(0.027)</td>
<td>(0.016)</td>
<td>(0.011)</td>
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<tr>
<td></td>
<td>(0.012)</td>
<td>(0.049)</td>
<td>(0.050)</td>
<td>(0.045)</td>
</tr>
<tr>
<td></td>
<td>(0.020)</td>
<td>(0.014)</td>
<td>(0.006)</td>
<td>(0.008)</td>
</tr>
</tbody>
</table>

Coefficients in bold are significant at a 5% level. Standard errors are robust to autocorrelation and heteroskedasticity using an HAC estimator for the variance and covariance matrix.
Figure 9: Wage inflation and unemployment, quarterly data, frequency decomposition
Then, in the last decade of the 20th century the estimates of $\delta^{S5}$ turn negative (last row of Figure 10), yielding a conventional PC effect over the shortest sub-sample, 1990Q1-2016Q4. When Equation (3) is estimated over the entire quarterly sample 1960Q1-2016Q4, $\delta_{1-S5}$ shows up with the wrong sign and statistically significant, but its impact is trivial in an economic sense. This is the reason for calling the PC vertical. Just as importantly, the growth of labor productivity and price inflation impact money wage inflation with statistically unit coefficients, as one would expect to hold in the long run.
Figure 10: Rolling window coefficients, UK, quarterly data, 1960:1-2016:4

(a) Unemployment D3  
(b) Labor productivity growth D3  
(c) Inflation D3  
(d) Unemployment D4  
(e) Labor productivity growth D4  
(f) Inflation D4  
(g) Unemployment D5  
(h) Labor productivity growth D5  
(i) Inflation D5  
(j) Unemployment S5  
(k) Labor productivity growth S5  
(l) Inflation S5

We use a rolling window using the 50% of the observations. Standard errors are robust to autocorrelation and heteroskedasticity using an HAC estimator for the variance and covariance matrix.
5 Discussion

With the Samuelson and Solow (1960) article, the focus of the Phillips Curve shifted from money wage inflation to price inflation, with the consequent corollary that policy could exploit a tradeoff between inflation and unemployment. The tradeoff issue was later dismissed by Phelps (1967), Friedman (1968), Sargent (1971) and Lucas (1972, 1973) and put to rest by the inflation of the 1970s. By the early Nineties, the state of the arts was that observable US data were inconsistent with a PC. Yet, “... a strikingly stable negative correlation exists over the business cycle, and recent theory indicates the Lucas-Sargent critique may not be empirically relevant. When we estimate the long-run trade-off as Gordon and Solow did, we find it is roughly one-for-one.” (King and Watson, 1994, p.168-170). The opposite holds for the UK. (Haldane and Quah, 1999, Fig 3) produce a conventionally sloped price inflation-unemployment scatter plot from 50 years of post-WWII monthly data. On the other hand, (Broadbent, 2014, Chart 2) shows a scatter plot of money wage inflation-unemployment for the years 1968-1992 that looks like a meandering curve drifting eastwardly. When we extend Broadbent’s scatter plot to the entire sample available, 1960Q1-2016Q4, the meandering pattern holds except for the years FEDERICO DEVI IDENTIFICARE GLI ANNI INDICATI IN VIOLA DOVE CURCA DISCENDE DA SINISTRA A DESTRA; see Figure A3 in the Appendix. The obvious inference is that wage and price PC are not the mirror image of each other. Our findings show that a wage PC relationship, over the long historical stretch, is observable in UK data only for certain periods, whereas it is negative, stable and strong in the medium-run frequency band.

The wage PC reemerged with Galí (2011) who embedded a staggered wage contract setup in a New Keynesian (NK) model. The implied NK wage PC is that money wage inflation responds positively to the expected one-period ahead wage inflation and negatively to the deviation of the average markup.

7The methodology employed for detecting effects at various frequencies is to filter the data with moving averages of different lengths and by placing constraints on specific points (Baxter and King, 1999; Christiano and Fitzgerald, 2003). King and Watson (1994) define the business-cycle component of the series by applying a band-pass filter isolating periodic components between one and half and eight years; for the long run, they apply a low-pass filter isolating periodicities beyond eight years; see their Figure 2 on page 168 and discussion on pages 169-170.

8The authors also report that the relationship is not stable over the 50 years: the Curve is virtually vertical from 1984 to 1980 and virtually flat afterwards. Furthermore, the Curve becomes vertical at business-cycle frequencies (Haldane and Quah (1999, Fig 5)), further highlighting the difference between wage and price PCs.

9Money wage inflation is adjusted for a measure of expected price inflation, against the unemployment rate.

10Staggered wage contracts—such as those in Fischer (1977), Taylor (1980) or Calvo (1983)—gave impetus to the development of the New Keynesian Phillips Curve, where current price inflation responds positively to the expected one-period price inflation and a measure of real economic activity.
from its desired value. However, in the empirical work based on post-war US quarterly data, money wage inflation is explained by one-period lagged price inflation and an autoregressive unemployment rate. Forward-looking NK price PC models have difficulty in explaining inflation dynamics in the data without an assumption of inflation persistence (Mavroeidis et al. (2014, p 130)). In the NK wage PC the lagged price inflation term is justified as a wage indexation factor, but in fact captures persistence, and so does the autoregressive structure of the unemployment rate.

The extent of persistence in the US wage PC emerges in Gallegati et al. (2011) who test Equation (3) with the same methodology of our paper over quarterly data from 1948Q1 to 2009Q2:

“...the highest and most significant effect of [the] unemployment rate on nominal wage growth occurs at intermediate scales...between 2 and 8 years, thus suggesting that the time of ‘pass through’ of the unemployment rate to wage inflation is in the business cycle frequency range...at the longest scale, corresponding to periods longer than 8 years, the estimated coefficient indicates a flattening of the wage Phillips curve, being otherwise more significant than any other frequency.” (Gallegati et al., 2011, p 497).

Our findings for the UK are in line with those of the US, except that the time of pass through of the unemployment rate to money wage inflation occurs in the medium-run range (8 to 16 years) rather than in the business-cycle range.

Much of the discussion about the Phillips Curve centers on its temporal instability. The high inflation rates of the 1970s and the disinflation transition in the first half of the 1980s are typically blamed for the breakdown of the PC relationship. In fact, in both sub-periods the observed scatter plots describe a positively sloped curve (Gali (2011, Fig 6)). Blanchard et al. (2015) estimates price PCs for 20 countries and finds that, for given expected inflation, the curve flattens until the early 1990s and then stabilizes. However, for the UK the slope is not statistically significant for either the years 1990-2014 or the years 2007-2014 (Table 6). (Cunliffe, 2017, Chart 6) fits trend lines through scatter plots of the UK money wage inflation-unemployment rate for the periods 1971-1997, 1998-2012 and 2013-2017 and concludes that the PC relationship has progressively shifted inward and flattened. Our estimates of δ (in the frequency range 11)

11The markup refers to the markup of the money wage with respect to the marginal rate of substitution between consumption and working. If the markup falls below its desired level, those workers who reset their money wages in a given year will experience a negative wage inflation. The NK wage PC is vertical when all workers renew their contracts each period. The Curve has the conventional negative slope: the smaller the proportion of workers renewing their contracts each period, the flatter in will be the Curve.

12More generally, a lagged rate of inflation may be interpreted as a proxy of the expected rate of inflation or price stickiness (inertia) stemming staggered wage contracts.
of 4 to 8 quarters) of Table 5, while not statistically significant, are suggestive of a flattening wage PC as one moves from longest sample of 1960Q1-2016Q4 to the shortest sample of 1990Q1-2016Q4. The rolling window estimates of δ\(^{12}\) in Figure 10 describe a sinusoid curve around a zero line. The point is that both at the aggregate level and at high frequencies the PC relationship is unstable over time. But, in the frequency range between 32 to 64 quarters (our medium run timescale), this time dependency disappears: the estimates of δ\(^{15}\) in the four different time periods of Table 5 range from -0.415 (with standard error of 0.133) to -0.679 (0.068).

The last and thorniest issue is why the PC relationship is stable primarily in the medium run. We do not have a satisfactory or complete answer. We limit ourselves to some observations on the matter. To start, labor is more a “quasi-fixed factor” than the variable input described in conventional microeconomics texts (Oi, 1962). Fixed hiring, firing and training costs—reflecting in part the power of the unions—are responsible for this semi-fixity. Wage contracts and monopolistic price settings impart stickiness. When staggered wage contracts were introduced in the macroeconomics literature, the objective was to mimic persistence in the data and create at the same time sufficient flexibility so that a credible monetary disinflation could be carried out with little or no economic contraction (Ball, 1994); a sort of having a cake and eat it too. But Führer and Moore (1995) discovered that contracts a la Taylor (1980), where the price level is an average of current and past contract wages, generate persistence in the level of prices but not in the rate of inflation.\(^{13}\) Consequently, we are left with imperfectly credible monetary policy or its interaction with wage contracts as an explanation for inflation persistence in the New Keynesian PC models, where money wage inflation responds to the expected rate of inflation (Ball, 1995). The specification of our paper is not consistent with those models and relies instead on the current rate of inflation, which is very strongly correlated with past rates of inflation. It may be an “ugly duckling” model but it does justice to the data.\(^{14}\)

6 Conclusion

The original Phillips Curve was not a short-run relationship. Phillips’ unorthodox data transformation was unfamiliar to economists of the time, but today

\(^{13}\)Driscoll and Holden (2004) start from the behavioral assumption that workers care more about being paid less than other workers than being paid more (a sort of asymmetric fairness) to generate a model of inflation persistence that occurs within certain bounds of the unemployment rate. Also near-rational expectations models have tried to arrive at inflation persistence.

\(^{14}\)On the point that rational expectations cannot explain persistence in NKPC models, see Mankiw (2001, C59) and Mavroeidis et al. (2014, p 172)
can be interpreted as a simple moving average with non-overlapping variable-width windows. Our paper goes back to this insight and uses an expansive UK sample of annual data, from 1861 to 2015, and quarterly post-WWII quarterly data, from 1960Q1 to 2016Q4, to explore the negative relationship between money wage inflation and the unemployment rate occurring at different frequency bands and time intervals. The two critical findings from the annual sample are that the wage PC is predominantly a medium-run phenomenon, comprised in the 8-to16-year frequency band, and that the curve disappears in the long run. Similar conclusions are reached for the post-WWII quarterly data. A negative and stable relationship between money wage inflation and unemployment occurs, again, in the medium-run frequency range of 32 to 64 quarters. While the PC effect is also present in the business-cycle frequency (16 to 32 quarters), it is unstable over different time intervals. A wage PC is not a mirror image of a price PC. Scatter plots of price inflation-unemployment in the post-WWII era produce a conventionally sloped curve, but not for money wage inflation-inflation. Possible causes of this difference may reside in variation in the labor share of total income, changes in productivity growth and a breakdown in the relationship between wage inflation and price inflation. The essential point is that over a long stretch of years a wage PC relationship is observable in UK data intermittently, whereas it is negative, stable and strong in the medium-run frequency band. The paper does not provide a theoretically satisfactory answer of why the PC relationship is stable in the medium-run frequency range. We refer to ongoing work in the literature on a source of wage and price stickiness, staggered wage contracts. The earlier promise that such contracts could explain nominal stickiness and retain sufficient flexibility to allow a credible monetary disinflation to be carried out with little or no economic loss of unemployment or output has not panned out. There is the alternative that monetary policy, the big driver in the growth of nominal magnitudes, suffers from very imperfect credibility. Clearly, additional research is required on the subject.
References


BIS, 2017. 87th Annual report.


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Appendix: Data

- The original database used by Phillips for the period 1860-1947 can be found in Wulwick (1996) Table 1 at page 427. For the left panel of Figure 1, we calculate:
  - Wage inflation is calculated as the log difference of the Money-Wage index (column 1).
  - Unemployment rate is the unemployment (column 3).

- We employ the A Millennium of macroeconomic data for the UK. The Bank of England’s collection of historical macroeconomic and financial statistics based on the work by Ryland et al. (2010).
  - Annual data for the period 1861-2015 are calculated as:
    * Wage inflation calculated as the log difference of Composite Average Weekly Earnings series taken from worksheet A.47
    * Unemployment rate is the Unemployment rate taken from the worksheet A.50
    * Labor productivity is the log difference of the Labour productivity per hour taken from worksheet A.56
    * Price inflation is calculated as the log difference of the GDP deflator at market prices taken from worksheet A.47
  - Quarterly data for the period 1960:1-2016:4 are calculated as:
    * Wage inflation calculated as the log difference of the Spliced Average Weekly Earnings series, 1919-2015 taken from worksheet Q.1
    * Unemployment rate is the Monthly unemployment rate taken from worksheet M.1 and transformed into quarterly frequency.
    * Labor productivity is calculated as the log difference of the Output per workers, seasonal adjusted.
    * Price inflation is calculated as the log difference of the GDP deflator at market prices taken from worksheet Q.1
Figure 11: Time series decomposition, UK, annual data, 1861-2016
Figure 12: Time series decomposition, UK, quarterly data, 1960-2016
Table 6: Dependent Variable: \( \Delta w_{jt} \), 1960:1-2016:4, UK, Bandpass filter, CF

\[
\begin{array}{cccc}
U_{it}^{D2} & 0.683 & -0.541 & -1.940 & -3.328 \\
(2.416) & (2.265) & (2.132) & (2.152) \\
U_{it}^{D3} & -0.540 & \textbf{-1.140} & 0.428 & 0.842 \\
(0.427) & (0.503) & (0.644) & (0.642) \\
U_{it}^{D4} & \textbf{-1.113} & 0.134 & \textbf{-0.868} & \textbf{-1.005} \\
(0.275) & (0.351) & (0.405) & (0.339) \\
U_{it}^{D5} & \textbf{-1.349} & \textbf{-1.392} & \textbf{-1.297} & \textbf{-0.977} \\
(0.075) & (0.083) & (0.127) & (0.124) \\
\end{array}
\]

\[
\begin{array}{cccc}
\Delta LP_{it}^{D2} & 0.024 & 0.206 & 0.529 & 0.453 \\
(0.175) & (0.146) & (0.144) & (0.133) \\
\Delta LP_{it}^{D3} & \textbf{0.227} & \textbf{0.238} & \textbf{0.238} & \textbf{0.372} \\
(0.086) & (0.058) & (0.060) & (0.077) \\
\Delta LP_{it}^{D4} & \textbf{0.770} & \textbf{0.420} & \textbf{0.639} & \textbf{0.839} \\
(0.072) & (0.137) & (0.141) & (0.114) \\
\Delta LP_{it}^{D5} & \textbf{-0.560} & \textbf{-0.524} & \textbf{-0.693} & \textbf{-0.741} \\
(0.078) & (0.078) & (0.177) & (0.185) \\
\end{array}
\]

\[
\begin{array}{cccc}
\pi_{it}^{D2} & -0.101 & -0.165 & -0.236 & -0.222 \\
(0.112) & (0.104) & (0.129) & (0.120) \\
\pi_{it}^{D3} & \textbf{-0.279} & 0.202 & \textbf{0.757} & \textbf{0.810} \\
(0.107) & (0.135) & (0.170) & (0.147) \\
\pi_{it}^{D4} & \textbf{0.517} & \textbf{1.137} & \textbf{1.210} & \textbf{1.284} \\
(0.093) & (0.147) & (0.078) & (0.071) \\
\pi_{it}^{D5} & \textbf{-0.319} & \textbf{-0.417} & \textbf{-0.455} & -0.143 \\
(0.066) & (0.074) & (0.118) & (0.130) \\
\end{array}
\]

Coefficients in bold are significant at a 5% level. Standard errors are robust to autocorrelation and heteroskedasticity using an HAC estimator for the variance and covariance matrix.